

Time limit: 15 minutes.

Instructions: This tiebreaker contains 5 short answer questions. You will submit answers to the problem as you solve them, and may solve problems in any order. You will not be informed whether your answer is correct until the end of the tiebreaker. You may submit multiple times for any of the problems, but **only the last submission for a given problem will be graded**. The participant who correctly answers the most problems wins the tiebreaker, with ties broken by the time of the last correct submission.

No calculators.

1. Wen finds 17 consecutive positive integers that sum to 2023. Compute the smallest of these integers.
2. Triangle $\triangle ABC$ has $\angle ABC = \angle BCA = 45^\circ$ and $AB = 1$. Let D be on \overline{AC} such that $\angle ABD = 30^\circ$. Let \overleftrightarrow{BD} and the line through A parallel to \overleftrightarrow{BC} intersect at E . Compute the area of $\triangle ADE$.
3. Mataio has a weighted die numbered 1 to 6, where the probability of rolling a side n for $1 \leq n \leq 6$ is inversely proportional to the value of n . If Mataio rolls the die twice, what is the probability that the sum of the two rolls is 7?
4. Let $N = 2^{18} \cdot 3^{19} \cdot 5^{20} \cdot 7^{21} \cdot 11^{22}$. Compute the number of positive integer divisors of N whose units digit is 7.
5. Compute the real solution for x to the equation $(4^x + 8)^4 - (8^x - 4)^4 = (4 + 8^x + 4^x)^4$.